### An Instruction Stream Compression Technique

P. Bird and T. Mudge

CSE-TR-319-96

November 1996

Computer Science and Engineering Division Room 3402 EECS Building

### THE UNIVERSITY OF MICHIGAN

Department of Electrical Engineering and Computer Science Ann Arbor, Michigan 48109-2122 USA



# An Instruction Stream Compression

Peter L. Bird Trevor N. Mudge

echnique

EECS Department University of Michigan

#### **Abstract**

The performance of instruction memory is a critical factor for both large, high performance applications and for embedded systems. With high performance systems, the bandwidth to the instruction cache can be the limiting factor for execution speed. Code density is often the critical factor for embedded systems.

In this report we demonstrate a straightforward technique for compressing the instruction stream for programs. After code generation, the instruction stream is analysed for often reused sequences of instructions from within the program's basic blocks. These patterns of multiple instructions are then mapped into single byte opcodes. This constitutes a compression of multiple, multi-byte operations onto a single byte. When compressed opcodes are detected during the instruction fetch cycle of program execution, they are expanded within the CPU into the original (multi-cycle) set of instructions. Because we only operate within a program's basic block, branch instructions and their targets are unaffected by this technique.

We provide statistics gathered from code generated for the Intel Pentium and the Power PC processors. We have found that incorporating a 1K decode ROM in the CPU we can reduce a program's code size between 45% and 60%.

#### 1. Introduction

Although it is usually true that a particular algorithm can be most efficiently implemented using hand-tuned assembly code, both the overhead in development, and the software life-cycle has made the use of high level languages essential for large-scale, evolving applications.

Compilers cannot truly *optimize* the generated code for any given program. This "sub-optimality" is manifest through larger code size and slower execution times than would be the case for hand crafted assembly code. The impact of slower execution times is readily apparent, and years of research have evolved better and more sophisticated optimization techniques for compilers. However, the *size* of the executing program also can have a severe impact upon program performance.

Embedded systems often use processors which have small addresses spaces for programs. Within this programming domain, the size of the program is often a limiting factor. Developers currently use assembly code to ensure applications fit within the program space constraints.

In high performance environments, program size is also a limiting factor. Most processors have an *instruction cache* for holding recently used program segments. The larger the program, the less likely it is that significant portions of its code will co-reside in the I-cache. An I-cache *miss* interrupts program execution while the missing code fragment is loaded from main memory, thereby reducing overall performance

Compressing a program's instruction stream would benefit a range of application domains both in the *size* of the program in memory, and in the *bandwidth* requirements for instruction fetch. In this report, we present a technique which addresses this issue.

For the remainder of this section, we will discuss patterns found in compiled programs. Section 2. gives a description of the hardware mechanism which implement the expansion of compressed programs. Section 3. presents the results of several experiments we performed on instruction pattern collection in a range of programs on different architectures. In Section 4. we provide our conclusions and discuss some future work. Raw data for our experiments can be found in the Appendix.

### 1.1 Instruction Patterns in Compiled Software

Compilers generate code using a Syntax Directed Translation Scheme (SDTS). [Aho-86]. Syntactic source code patterns are mapped onto templates of instructions which implement the appropriate semantics. Consider, for example, a schema to translate a subset of integer arithmetic:

An Instruction Stream Compression Technique CSE-TR-319-96

In both of these patterns, the expression subtrees on the RHS of the productions return registers which is used by the arithmetic operation. The register purpoer holding the result of the operation (\$1) is passed up the parse tree for use in the parent operation.

Compilers reuse instruction templates throughout all generated programs. The only difference in instruction sequences are the register numbers in arithmenic instructions and operand offsets for *load* and *store* instructions. As a consequence, object modules are generated with many common sub-sequences of instructions. There is a high degree of redundancy in the encoding of a program.

The emergence of RISC architectures exacerbates this problem. A RISC instruction set generally trades efficient encodings for efficient decoding. That is, instructions have fixed width (i.e. always 4 bytes). Those fields which are not required for certain operations are wasted.

Newer programming languages encourage the increase of redundancy in programs. One example of this trend can be seen in applications developed using Object Oriented programming techniques. *Information hiding* is one organizational strategy (among many) used for OOP. The implementation of an object is hidden within the private namespace of the class, with member functions used as the interface to the object. Often, these member functions are simple access routines which reference private data structures. These short code sequences are also pattern templates, similar to the SDTS of a compiler.

### 2. Description of Code Compression Technique

After code generation and register allocation, we analyse the generated code stream to search for patterns. This pattern search is made over all instruction sequences of all basic blocks of the program<sup>1</sup>. All patterns of all lengths are compared. The pattern checker finds all distinct patterns, and counts their frequency of occurrence throughout the code stream. Those patterns with the highest frequency of usage are assigned an opcode, and the sequence of instructions for that opcode is saved in a ROM in the CPU. This decode table could be included as a part of the process state, much like a page table.

<sup>1.</sup> A basic block starts at a label (or after a branch operation) and ends with a branch operation (or another label).

During instruction fetch, the decoder checks the opcode of the incoming instruction. If the opcode indicates an uncompressed instruction, then instruction decode and execution proceeds in a conventional fashion. When the decoder encounters a compressed instruction, the entire sequence of instructions is retrieved from the ROM and dispatched through the execution pipeline one instruction per cycle. Instruction fetch from the program memory stream is stalled until the sequence completes.

#### 2.1 Discussion

Perhaps the biggest limitation of the implementation described above is that it appears to require a *pre-decode* phase of the instruction pipeline of a processor (to determine if the instruction is compressed or not). This limitation might be ameliorated if the processor maintains a short instruction queue whose members were checked for compression. This check could be performed during the μ-op expansion phase of the Pentium-Pro instruction pipeline [Micro-95].

This does not help the case where the compressed instruction is the target of a branch instruction. In this case, if the target instruction were held in the ROM table (following the branch instruction), pre-decode could be accomplished without incurring a delay in the instruction pipeline.

Although the ISA form of instructions can be held in the ROM table (resulting in a smaller table), a post-decoded form of the instruction could be used to speed instruction processing.

In our model the ROM table is specific to an application. When this is feasible, it results in the best compression behavior. The disadvantage, of course, is that the processor is thereafter configured to that application. For embedded processors this is not a limitation, since a single application is usually 'burned' into a ROM and run for the lifetime of the system. This is obviously unsatisfactory for more general systems. There are alternative models for implementation.

As mentioned above, the decode table could be made a part of the state of a process (much like the page tables capture the virtual memory structure of a process). This would allow the ROM to readily change for different applications.

A library of sequences could become a part of the ISA for a given implementation of an architecture machine. This could permit a manufacturer to maintain a common ISA for all machines, yet 'tune' a specific processor implementation for a given application domain (such as multi-media). Compilers (or post-compilation processors) could translate instruction sequences into the opcodes of the library for the implementation.

The ROM table itself represents a significant cost in silicon area in the CPU. There are several ways one could implement the ROM:

• Use a fixed width table (i.e. all instruction sequences are the length of the longest sequence).

Clearly, this is wasteful of ROM space, since short sequences will have unused slots.

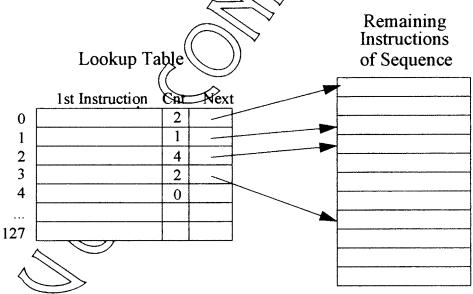
• Partition the ROM table into sets of sequences. The first N stots would be 2 instruction lengths, the next M slots would be 3 instruction lengths, etc.

Although this is less wasteful than the first scheme, it would still be wasteful, since it is unlikely that any given set of patterns would fit neatly into the assigned partitions.

• Use an *index* table to indicate starting ROM position and sequence length.

This would more efficiently use space than the first two schemes, but would require two ROM accesses before the first instruction would be available for execution. This is likely to be an unacceptable overhead (especially in high performance applications).

We need to both minimize its size, and minimize the cost of looking up instructions. We can use a form of the preceding model, where the 1st instruction of the sequence is a part of the index lookup. A compressed opcode is used to index into the *Lookup Table*. The first instruc-



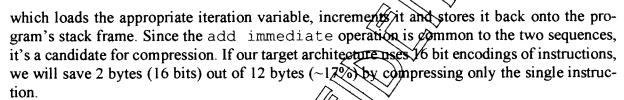
tion of the sequence is drawn from the *lookup table* and sent to the instruction execution pipeline. The *count* of the remainder of the sequence is drawn from the table and using the index of the *next* instruction, the remaining instructions of the sequence are retrieved from a secondary ROM table.

In the simplest case, even single instruction encodings are effective. Consider the following program fragment:

**An Instruction Stream Compression Technique** CSE-TR-319-96

Each loop would contain the instruction sequence.

$$\begin{array}{lll} \text{Load} & & \text{R}_n, \text{offset}_{\{i,j\}} \; (\text{R}_{base}) \\ \text{Addi} & & \text{R}_n, =1 \\ \text{Store} & & \text{R}_n, \text{offset}_{\{i,j\}} \; (\text{R}_{base}) \end{array}$$



When we permit compression of sequences of instructions the results are more dramatic. If both loops use the same iteration variable (whether on the stack or held in a register), then the two increment sequences would be equivalent, and could be reduced to a single byte. The two 6 byte sequences would be reduced to 2 bytes (7.83% savings).

We have intentionally ignored the issue of optimizations in this example. For example, in both loop instances the iteration variable sould be assigned to a register and never written back to the stack frame. However, ever with optimizations the compression technique discussed here are applicable.

Further compression would be possible were the compiler aware that the optimization was available, and generated a program's code sequences accordingly.

Large register sets are disadvantageous to this technique. Sequence patterns are formed by looking only at the distinct bit patterns of instructions (and not the operations being performed). Using different registers for the same sequence of operations would result in distinct patterns. However, this issue didn't seem to have the impact we expected as our experimental results show for the Power PC (Section 3.).

All of the discussion thus far has focussed upon the *static* characteristics of programs. Although we have not investigated *dynamic* behavior in detail for this paper, it should be clear that dynamic usage counts of instruction traces (collected by a profiler) could be used for pattern construction in conjunction with *static* pattern construction.

As mentioned above, instruction cache pressure is a major constraint for high performance program execution [Uhlig-95]. An I-cache miss will stall the processor, while the instruction memory access bandwidth limits the rate at which new instructions can be delivered to the processor. Because this scheme reduces the size of programs, it effectively increases the effective

size of an I-cache for the same program fragment (a code stream is dynamically expanded within the CPU rather than redundantly occupying precious cache lines). Moreover, since fewer bytes are transferred from program memory to the I-cache, the instruction memory bandwidth requirements of the program are reduced.

We should note that while this technique is orthogonal to instruction level parallelism techniques, they could be combined (see Section 4. below).

### 3. Experiments

We analysed 3 programs on two types of processors to determine the impact of *static* instruction sequence compression upon program size. The three programs were:

- The GO program from the SPEC benchmarks [SPEC 95].
- A compiler for B# (a C-like programming language used in our compiler class).
- A large module from an image processing work bench [C&G 96].

The GO program was compiled with the GCC compiler for a Power PC. The other two programs were compiled using Microsoft's Visial C++, version 4.1, for the Intel Pentium. The compiler is written using only C language features (within the framework of LEX and YACC), while the image processing module draws very heavily from the object oriented components of C++, such as overloading, member access functions, virtual functions, etc.

Although all programs displayed long instruction sequence patterns (up to 20 instructions in the image processing module) we restricted our pattern search to sequences from 1 to 8 instructions. The data for the three programs is summarized in the following table. The sizes of the ROM tables include only the raw instruction sequences and do not incorporate all fields described in Section 2.1 above. Code sizes include the size of the ROM table along with the compressed program.

	GO	Compiler	Image
Processor	Power PC	Pentium	Pentium
Basic Blocks	10213	2044	//4686
Uncompressed Bytes	219236	32422	60273
Total Instructions	54809 /	8919	18815
Distinct Instructions	13737	1914	3978
Distinct Patterns (length 1 to 8)	130952	15823	23937
Code size after compressing 1st 16 Patterns	8%	76.1%	62.5%
ROM size (in bytes) for 1st 16 Patterns	464	147	124
Code Size using 1K of ROM	5580	52.6%	40.3%
Code size after compressing 1st 128 patterns	43/3%	49.3%	40.1%
ROM size (in bytes) for 1st 128 patterns	1920	1613	1039

#### 3.1 Discussion

The results of our analysis are encouraging. Compressing only 16 patterns and using a very modest ROM size, we were able to reduce programs by 24% to 38% of their original size. Using a 1K ROM tables, programs were compressed to between 45% and 60% of the original size. These represent very modest investments in silicon area.

# 4. Conclusion and Directions for Future Work

We have outlined a technique for generating dense program encodings. Our technique exploits exactly those instruction sequence patterns which are repeated within a particular program.

We have discussed in Section 2.1) ways this technique could be enhanced by adding a predecode phase of instruction execution. A more detailed study of the problem is required.

We have shown that there is a high degree of regularity of patterns for different applications compiled on different architectures. It would be interesting to see whether patterns exist which are

- idiomatic to specific applications (integer vs. floating point, data base vs. multimedia, etc.)
- · specific to compilers
- idiomatic to machines.

If the latter case is true, then this technique could be useful for any general purpose machine in reducing its instruction fetch bottleneck.

27 November 1996

We believe it would be very interesting to examine the *dynamic* behavior of a program when analysing patterns. By incorporating a profiler, this process is no more difficult than collecting *static* patterns. Our ROM table (containing a compressed tag following a branch instruction), could augment or even replace a branch target buffer. Essentially, our compressed instruction would become a *highly-likely* program trace path.

It is interesting to note the relationship of our work with *Trace Scheduling* [Ellis-85], a technique for enhancing program parallelism which was derived from microcode compaction. The focus of trace scheduling is to expose all machine operations to the compiler, thereby increasing the set of operations which can be re-combined for parallel execution. One disadvantage of compiler control of micro-operations is the added cost of program memory required to specify the control of all operations every cycle. Although it is fruitful to open the box" to expose the possible parallel operations, we believe that a final set of sommon parallel operations can be distilled to a small number of fixed actions. It would make sense to collapse these operations onto a small set of opcodes thereby reducing the instruction memory requirements of the program.

### **Bibliography**

Aho-86	A. Aho, R. Seth and J. Ullman, Compiler: Principles, Techniques
	and Tools, Addison-Wesley, 1986.
C&G 96	Image Processing Workbench, C&G Software Engineering, Ann
	Arbor, MI. 1996.
Ellis-85	J. Ellis, Bulldog: A Compiler for VLIW Architectures, ACM Dis-
	tinguished Dissertation, MIT Press, 1985.
Micro-95	/Intel's PoUses Decoupled Superscalar Design," Microprocessor
	Report 9(2), 16 February 1995.
SPEC-95	Spec Benchmarks, 1995.
Uhlig-95	Ryhlig, Trap-Driven Memory Simulation, Ph.D dissertation,
	EECS Department, University of Michigan, Ann Arbor, MI, 1995.
<i>\</i> \ \ \	

# **Appendix**

To give the reader an idea of the impact of pattern sequences on program compression, we here

present the raw data of our analyser for the 3 programs we studied.

### **GO Program**

54809	Instructions

219236 bytes in program

13737 distinct instructions

4203 labels

10213 basic blocks

130952 distinct parterns of length 1 to 8

				Cimulative	ROM		Program
	Bytes in	Instructions	Use	Dylon	Table	Program Size	Size with
#	Pattern	in Pattern	Count	Saved	Size	(vs. Original)	ROM Table
1	4	1	1900	\$700	4	97.4%	97.4%
2	32	8	477	1187	36	94.9%	94.9%
3	32	8	((174	16581	68	92.4%	92.5%
4	32	8 ^	169	21820	100	90.0%	90.1%
5	32	8,	169	27059	132	87.7%	87.7%
6	32	8	154	31833	164	85.5%	85.6%
7	32	///8	> 154	36607	196	83.3%	83.4%
8	32	<b>4</b> /8	129	40606	228	81.5%	81.6%
9	32	18	129	44605	260	79.7%	79.8%
10	32 (	<b>)</b> 8	107	47922	292	78.1%	78.3%
11	<b>42</b>	<b>€</b> 8	107	51239	324	76.6%	76.8%
12	( 32	8	97	54246	356	75.3%	75.4%
13	32	8	97	57253	388	73.9%	74.1%
14	4	1	928	60037	392	72.6%	72.8%
15	32	8	76	62393	424	71.5%	71.7%
16	32	8	76	64749	456	70.5%	70.7%
17	8	2	288	66765	464	69.5%	69.8%
18	32	8	62	68687	496	68.7%	68.9%
19	32	8	62	70609	528	67.8%	68.0%
20	4	1	595	72394	532	67.0%	67.2%
21	4	1	563	74083	536	66.2%	66.5%

22	12	3	150	75733	548	65.5%	65.7%
23	32	8	46	77159	580	64.8%	65.1%
24	32	8	46	78585	612	64.2%	64.4%
25	16	4	85	79860	628	63.6%	/93.9%
26	16	4	82	81090	644	63.00	<b>√</b> 63.3%
27	32	8	37	82237	676	A 62.5%	62.8%
28	32	8	37	83384	708 /	62.0%	62.3%
29	16	4	75	84509	724	61.5%	61.8%
30	20	5	59	85630	74	60.9%	61.3%
31	4	1	372	86746	748	60.4%	60.8%
32	4	1	352	87802	152	<b>&gt;</b> 60.0%	60.3%
33	20	5	55	88847		59.5%	59.8%
34	24	6	40	89767	799	59.1%	59.4%
35	4	1	294	90649	800	58.7%	59.0%
36	32	8	27	<914 <b>8</b> 6	832	58.3%	58.7%
37	32	8	27 4	<del>(3)</del> 333	864	57.9%	58.3%
38	4	1	278	93157	868	57.5%	57.9%
39	24	6	36((	98985	892	57.1%	57.5%
40	4	1	270	94795	896	56.8%	57.2%
41	4	1	. \267	> 95596	900	56.4%	56.8%
42	16	4	53	96391	916	56.0%	56.5%
43	4	الميرا .	<b>331</b>	97084	920	55.7%	56.1%
44	4	_1	219	97741	924	55.4%	55.8%
45	4	[//]1	<b>→</b> 214	98383	928	55.1%	55.5%
46	32	18	20	99003	960	54.8%	55.3%
47	32 ((	18/2	20	99623	992	54.6%	55.0%
48	32	<b>J</b> 8	20	100243	1024	54.3%	54.7%
49	32	8	20	100863	1056	54.0%	54.5%
50	32	> 8	19	101452	1088	53.7%	54.2%
51	8	2	82	102026	1096	53.5%	54.0%
52	4	1	187	102587	1100	53.2%	53.7%
53	4	1	186	103145	1104	53.0%	53.5%
54	32	8	18	103703	1136	52.7%	53.2%
55	32	8	17	104230	1168	52.5%	53.0%
56	32	8	17	104757	1200	52.2%	52.8%
57	4	1	165	105252	1204	52.0%	52.5%
58	4	1	161	105735	1208	51.8%	52.3%

59	4	1	155	106200	1212	51.6%	52.1%
60	28	7	17	106659	1240	51.3%	51.9%
61	4	1	152	107115	1244	51.1%	51.7%
62	4	1	145	107550	1248	50.9%	<b>/</b> \$1.5%
63	4	1	140	107970	1252	50.80	51.3%
64	12	3	38	108388	1264	~ \$0.69¢	√ 51.1%
65	4	1	139	108805	1268	50.4%	50.9%
66	4	1	137	109216	1272	50.2%	50.8%
67	4	1	135	109621	1276	50.0%	50.6%
68	32	8	13	110024	17598	49.8%	50.4%
69	32	8	13	110427	1340	<b>/</b> 49.6%	50.2%
70	4	1	134	110829	THEY'	49.4%	50.1%
71	4	1	133	111228	1348	49.3%	49.9%
72	12	3	36	11/1674	1360	49.1%	49.7%
73	4	1	130	(41)2014	1364	48.9%	49.5%
74	4	1	128	( <del></del>	1368	48.7%	49.4%
75	4	1	125	112273	1372	48.6%	49.2%
76	4	1	123(	3142	1376	48.4%	49.0%
77	4	1	<b>P10</b>	13472	1380	48.2%	48.9%
78	4	1	108	→ 113796	1384	48.1%	48.7%
79	4	1 🖒	105	114111	1388	48.0%	48.6%
80	4	1/-	185	114426	1392	47.8%	48.4%
81	4	_1	105	114741	1396	47.7%	48.3%
82	8	[1/2	<b>→</b> 45	115056	1404	47.5%	48.2%
83	32	8	10	115366	1436	47.4%	48.0%
84	32 ((	18/2	10	115676	1468	47.2%	47.9%
85	16	Jg .	20	115976	1484	47.1%	47.8%
86	16	4	20	116276	1500	47.0%	47.6%
87		> 1	97	116567	1504	46.8%	47.5%
88	16	4	19	116852	1520	46.7%	47.4%
89	4	1	94	117134	1524	46.6%	47.3%
90	4	1	94	117416	1528	46.4%	47.1%
91	4	1	93	117695	1532	46.3%	47.0%
92	32	8	9	117974	1564	46.2%	46.9%
93	32	8	9	118253	1596	46.1%	46.8%
94	32	8	9	118532	1628	45.9%	46.7%
95	32	8	9	118811	1660	45.8%	46.6%

96	8	2	39	119084	1668	45.7%	46.4%
97	4	1	90	119354	1672	45.6%	46.3%
98	4	1	90	119624	1676	45.4%	46.2%
99	4	1	88	119888	1680	45.3%	/\$6.1%
100	4	1	84	120140	1684	45.20	<b>₹46.0%</b>
101	4	1	83	120389	1688	A5 190	45.9%
102	20	5	13	120636	1708	45.0%	45.8%
103	8	2	35	120881	1716	44.9%	45.6%
104	16	4	16	121121	1737	44.8%	45.5%
105	4	1	78	121355	1736	¥4.6%	45.4%
106	4	1	78	121589	1240	<b>) 44.5%</b>	45.3%
107	4	1	78	121823	<b></b>	44.4%	45.2%
108	8	2	33	122054	1752	44.3%	45.1%
109	12	3	21	12225	1764	44.2%	45.0%
110	20	5	12	V1552213	1784	44.1%	44.9%
111	4	1	74	( 2222525 )	1788	44.0%	44.8%
112	4	1	74	122957	1792	43.9%	44.7%
113	4	1	73((	123176	1796	43.8%	44.6%
114	32	8		23393	1828	43.7%	44.6%
115	4	l	72	> 123609	1832	43.6%	44.5%
116	4	1 6	72	123825	1836	43.5%	44.4%
117	4	الميا	74	124038	1840	43.4%	44.3%
118	4	_1	71	124251	1844	43.3%	44.2%
119	4	[[]	$\rightarrow$ 70	124461	1848	43.2%	44.1%
120	8	- 18	30	124671	1856	43.1%	44.0%
121	12 ((	13/2	19	124880	1868	43.0%	43.9%
122	12	<i>)</i>	19	125089	1880	42.9%	43.8%
123	1	1	69	125296	1884	42.8%	43.7%
124		> 1	68	125500	1888	42.8%	43.6%
125	8	2	29	125703	1896	42.7%	43.5%
126	4	1	65	125898	1900	42.6%	43.4%
127	16	4	13	126093	1916	42.5%	43.4%
128	4	1	64	126285	1920	42.4%	43.3%

# **B# Compiler**

		0/1/	111311	uctions			
		32423	byte	s in program		^	$\sim$
		1914	disti	nct instructio	ns		$\forall$
		867	labe	ls			$\Rightarrow$
		2044		c blocks			
		15823		nct patterns o	flenat	V 10 8	
		15025	ursa	•	Z <del>-</del>	7,000	
	Bytes in	Instructions	Use	Cumulative Bytes	ROM Vable	Simon Simo	Program
#	Pattern	in Pattern	Count	Saved	Size	Program Size  Ws. Original)	Size with ROM Table
1	5	1	311	1244		96.2%	96.2%
2	5	1	197	2032	<b>\\\\</b>	93.7%	93.8%
3	11	3	70	7787	>21	91.6%	91.6%
4	8	2	86	<b>43334</b>	29	89.7%	89.8%
5	8	2	68	( <del>-3810</del> )	37	88.2%	88.4%
6	3	1	211/	*232	40	86.9%	87.1%
7	22	8	20((	652	62	85.7%	85.8%
8	8	2	/32 ×	5016	70	84.5%	84.7%
9	5	1	86_	> 5360	75	83.5%	83.7%
10	5	1	84	5696	80	82.4%	82.7%
11	13	3	287	6032	93	81.4%	81.7%
12	11	$\sim$ 3	33	6362	104	80.4%	80.7%
13	3	///\lambda	7 163	6688	107	79.4%	79.7%
14	6	THE	65	7013	113	78.4%	78.7%
15	19 ((	14~	18	7337	132	77.4%	77.8%
16	7	$\mathcal{J}$	51	7643	139	76.4%	76.9%
17	18	2	38	7909	147	75.6%	76.1%
18	( <u>)</u>	> 5	65	8169	152	74.8%	75.3%
19	10	2	27	8412	162	74.1%	74.6%
20	3	1	116	8644	165	73.3%	73.8%
21	24	8	10	8874	189	72.6%	73.2%
22	5	1	55	9094	194	72.0%	72.6%
23	9	3	26	9302	203	71.3%	71.9%
24	15	6	13	9484	218	70.7%	71.4%
25	35	8	5	9654	253	70.2%	71.0%
26	5	1	42	9822	258	69.7%	70.5%

8919 Instructions

27	5	1	41	9986	263	69.2%	70.0%
28	14	3	12	10142	277	68.7%	69.6%
29	8	2	22	10296	285	68.2%	69.1%
30	5	1	38	10448	290	67.8%	/68.7%
31	9	6	19	10600	299	67.80	<b>√68.2%</b>
32	6	2	29	10745	305	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	<sup>⇒</sup> 67.8%
33	5	1	35	10885	310	66.4%	67.4%
34	8	2	20	11025	318	06.0%	67.0%
35	24	8	6	11163	342	65.6%	66.6%
36	18	5	8	11299	<b>760</b>	65.2%	66.3%
37	6	2	27	11434	366	/> 64.7%	65.9%
38	6	2	27	11569	-345 ×	64.3%	65.5%
39	7	3	22	11700	379	63.9%	65.1%
40	13	3	11	1/8/33	392	63.5%	64.7%
41	11	2	13	~11963_	403	63.1%	64.3%
42	33	7	4	( <del>-13</del> 051)	436	62.7%	64.1%
43	7	2	21	15317	443	62.3%	63.7%
44	6	1	24((	12337	449	61.9%	63.3%
45	16	5	<b>8</b>	12457	465	61.6%	63.0%
46	5	1	28	<b>&gt;</b> 12569	470	61.2%	62.7%
47	5	1 6	28	12681	475	60.9%	62.4%
48	3	1/-	35	12791	478	60.5%	62.0%
49	12	2	10	12901	490	60.2%	61.7%
50	12	[[]4	> 10	13011	502	59.9%	61.4%
51	7		18	13119	509	59.5%	61.1%
52	3 ((	1/2	54	13227	512	59.2%	60.8%
53	16		7	13332	528	58.9%	60.5%
54	A 44	4	8	13436	542	58.6%	60.2%
55	(6)	> 2	20	13536	548	58.3%	59.9%
56	26	6	4	13636	574	57.9%	59.7%
57	3	2	47	13730	577	57.7%	59.4%
58	3	3	47	13824	580	57.4%	59.2%
59	24	7	4	13916	604	57.1%	58.9%
60	11	2	9	14006	615	56.8%	58.7%
61	16	5	6	14096	631	56.5%	58.5%
62	3	1	43	14182	634	56.3%	58.2%
63	7	2	14	14266	641	56.0%	58.0%

64	15	3	6	14350	656	55.7%	57.8%
65	5	1	20	14430	661	55.5%	57.5%
66	5	1	20	14510	666	55.2%	57.3%
67	2	1	78	14588	668	55.0%	57.1%
<b>68</b>	2	1	78	14666	670	54.800	<b>√</b> 56.8%
69	3	2	39	14744	<b>67</b> 3	~ True 5000	<sup>√</sup> 56.6%
70	27	8	3	14822	700	54.3%	56.4%
71	8	3	11	14899	708	34.6%	56.2%
72	3	1	38	14975	74	53.8%	56.0%
73	4	3	25	15050	17/5	53.6%	55.8%
74	7	1	12	15122	1822	/> 53.4%	55.6%
75	5	1	18	15194	<del></del>	53.1%	55.4%
76	7	2	12	15265	734	52.9%	55.2%
77	13	3	6	15358	747	52.7%	55.0%
78	10	5	8	<15×10	757	52.5%	54.8%
79	8	2	10	<del></del>	765	52.3%	54.6%
80	7	2	11	13546	772	52.1%	54.4%
81	6	2	13((	15611	778	51.9%	54.3%
82	3	1	730	<b>1</b> 5671	781	51.7%	54.1%
83	3	1	(30	15731	784	51.5%	53.9%
84	6	1 🏠	12	15791	790	51.3%	53.7%
85	13	4	13	15851	803	51.1%	53.6%
86	31	8	2	15911	834	50.9%	53.5%
87	31	///8	> ₂	15971	865	50.7%	53.4%
88	30	8	2	16029	895	50.6%	53.3%
89	30 ((	18/2	2	16087	925	50.4%	53.2%
90	5	$\bigcirc$	14	16143	930	50.2%	53.1%
91	13	l	28	16199	933	50.0%	52.9%
92	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	> 3	4	16255	948	49.9%	52.8%
93	15	5	4	16311	963	49.7%	52.7%
94	29	8	2	16367	992	49.5%	52.6%
95	29	8	2	16423	1021	49.3%	52.5%
96	7	1	9	16477	1028	49.2%	52.4%
97	10	4	6	16531	1038	49.0%	52.2%
98	10	5	6	16585	1048	48.8%	52.1%
99	19	5	3	16639	1067	48.7%	52.0%
100	19	5	3	16693	1086	48.5%	51.9%

101	19	5	3	16747	1105	48.3%	51.8%
102	28	7	2	16801	1133	48.2%	51.7%
103	28	7	2	16855	1161	48.0%	51.6%
104	14	5	4	16907	1175	47.9%	<b>/</b> 51.5%
105	27	8	2	16959	1202	47.00	<b>√</b> 51.4%
106	27	8	2	17011	1229	A7.5%	51.3%
107	18	3	3	17062	1247	47.4%	51.2%
108	6	2	10	17112	1253	47.2%	51.1%
109	26	8	2	17162	1279	47.1%	51.0%
110	5	1	12	17210	<i>Y284</i>	¥6.9%	50.9%
111	5	1	12	17258	1289	<b>) 46.8%</b>	50.7%
112	5	1	12	17306	<b></b>	46.6%	50.6%
113	13	2	4	17352	1307	46.5%	50.5%
114	13	3	4	17/402	1320	46.3%	50.4%
115	25	5	2	17450	1345	46.2%	50.3%
116	25	5	2 4	<del></del>	1370	46.0%	50.3%
117	17	6	3	17546	1387	45.9%	50.2%
118	13	7	4((	17594	1400	45.7%	50.1%
119	25	8	$\sqrt{2}$	JY7642	1425	45.6%	50.0%
120	25	8	(le	> 17690	1450	45.4%	49.9%
121	24	8	2	17736	1474	45.3%	49.8%
122	24	السيح	2	17782	1498	45.2%	49.8%
123	24	8	2	17828	1522	45.0%	49.7%
124	47	[//8	$\rightarrow$ 1	17874	1569	44.9%	49.7%
125	6	18	9	17919	1575	44.7%	49.6%
126	16 ((	13/2	3	17964	1591	44.6%	49.5%
127	16	<i>J</i> 3	3	18009	1607	44.5%	49.4%
128	1	4	9	18054	1613	44.3%	49.3%
		>					

# **Image Processing Module**

18815	Instructions

60273 bytes in program

3978 distinct instructions

2028 labels

4686 basic blocks

23937 distinct patterns of length to 8

	23937 distinct patterns of length to 8							
				Cumulative	ROM		Program	
	Bytes in	Instructions	Use	Bytes	∠Marble `	Program Size	Size with	
#	Pattern	in Pattern	Count	Saved	Sixe	/ws. Original)	ROM Table	
1	14	3	267	3471	- A	94.2%	94.3%	
2	14	6	232	6487	28	89.2%	89.3%	
3	6	4	411	8842	<b>&gt;</b> 34	85.8%	85.9%	
4	9	5	216	<10270	43	83.0%	83.0%	
5	7	1	268	<del>₹118</del> 28, ✓	50	80.3%	80.4%	
6	3	1	736	13350	53	77.9%	77.9%	
7	12	7	118(	14648	65	75.7%	75.8%	
8	7	1	208	15896	72	73.6%	73.7%	
9	5	1	267	→ 16964	77	71.9%	72.0%	
10	5	3	267	18032	82	70.1%	70.2%	
11	3		486	19004	85	68.5%	68.6%	
12	4	A	257	19775	89	67.2%	67.3%	
13	4	[//2	→ <sub>245</sub> .	20510	93	66.0%	66.1%	
14	5	$\mathscr{N}_{\widehat{\square}}$	156	21134	98	64.9%	65.1%	
15	12 ((	13	50	21684	110	64.0%	64.2%	
16	9	<u>J</u>	67	22220	119	63.1%	63.3%	
17	13	1	129	22736	124	62.3%	62.5%	
18	( )	> 1	129	23252	129	61.4%	61.6%	
19	3	1	238	23728	132	60.6%	60.9%	
20	6	2	85	24153	138	59.9%	60.2%	
21	16	4	28	24573	154	59.2%	59.5%	
22	13	6	35	24993	167	58.5%	58.8%	
23	3	1	183	25359	170	57.9%	58.2%	
24	6	5	73	25724	176	57.3%	57.6%	
25	8	2	49	26067	184	56.8%	57.1%	
26	5	1	84	26403	189	56.2%	56.5%	

27	5	1	84	26739	194	55.6%	56.0%
28	9	5	42	27075	203	55.1%	55.4%
29	9	5	41	27403	212	54.5%	54.9%
30	12	4	24	27667	224	51 1%	/54.5%
31	19	4	14	27919	243	53.00	<b>₹</b> 54.1%
32	19	8	14	28171	262	\$3.3 <b>x</b>	<sup>7</sup> 53. <b>7%</b>
33	5	1	62	28419	267 /	52.8%	53.3%
34	8	2	35	28664	275	52.4%	52.9%
35	5	1	60	28904	280	52.0%	52.5%
36	3	1	113	29130	783	51.7%	52.1%
37	16	6	14	29340	×200 /	/ <sup>&gt;</sup> 51.3%	51.8%
38	7	1	33	29538	306	51.0%	51.5%
39	8	2	28	29734	3))	50.7%	51.2%
40	8	2	28	299930	322	50.3%	50.9%
41	7	3	30	√30176	329	50.0%	50.6%
42	8	2	25 \( \zera \)	<del></del>	337	49.8%	50.3%
43	7	2	28	304.53	344	49.5%	50.0%
44	7	3	28((	30621	351	49.2%	49.8%
45	4	1	/54	<b>3</b> 0783	355	48.9%	49.5%
46	12	4	(14)	> 30937	367	48.7%	49.3%
47	10	2	16	31081	377	48.4%	49.1%
48	7	السر2	24	31225	384	48.2%	48.8%
49	19	6	8	31369	403	48.0%	48.6%
50	12	[[7]	> 13	31512	415	47.7%	48.4%
51	11	13	14	31652	426	47.5%	48.2%
52	11 ((	13/2	14	31792	437	47.3%	48.0%
53	12		12	31924	449	47.0%	47.8%
54	A FO	$\smile_2$	14	32050	459	46.8%	47.6%
55	(32)	> 7	6	32176	481	46.6%	47.4%
56	5	1	30	32296	486	46.4%	47.2%
57	10	2	13	32413	496	46.2%	47.0%
58	9	3	14	32525	505	46.0%	46.9%
59	7	2	18	32633	512	45.9%	46.7%
60	3	1	50	32733	515	45.7%	46.5%
61	4	2	33	32832	519	45.5%	46.4%
62	6	1	18	32922	525	45.4%	46.2%
63	7	3	15	33012	532	45.2%	46.1%

64	19	6	5	33102	551	45.1%	46.0%
65	3	1	44	33190	554	44.9%	45.9%
66	3	1	44	33278	557	44.8%	45.7%
67	12	7	8	33366	569	44.600	/45.6%
68	4	1	29	33453	573	44.500	<b>₹</b> 45.4%
69	7	2	14	33537	<b>58</b> 0	A 44.4 4	45.3%
70	7	3	14	33621	587	44.2%	45.2%
71	15	7	6	33705	602	44.1%	45.1%
72	3	1	41	33787	605	43.9%	44.9%
73	5	2	20	33867	100	43.8%	44.8%
74	17	7	5	33947	627	/> 43.7%	44.7%
75	12	3	7	34024	<b>₹39</b>	43.6%	44.6%
76	12	3	7	34160	68)	43.4%	44.5%
77	5	1	19	34,8777	656	43.3%	44.4%
78	5	1	19	<b>\34253</b>	661	43.2%	44.3%
79	16	8	5 4	( <del>- 33</del> 378 )	677	43.0%	44.2%
80	5	1	18	34400	682	42.9%	44.1%
81	5	1	18((	34472	687	42.8%	43.9%
82	5	1	81	34544	692	42.7%	43.8%
83	13	5	(6)	> 34616	705	42.6%	43.7%
84	4	1 🖒	23	34685	709	42.5%	43.6%
85	5	الليها	177	34753	714	42.3%	43.5%
86	5	1	17	34821	719	42.2%	43.4%
87	5	[[]	> 17	34889	724	42.1%	43.3%
88	5		17	34957	729	42.0%	43.2%
89	12 ((	13/2	6	35023	741	41.9%	43.1%
90	7		11	35089	748	41.8%	43.0%
91	15		16	35153	753	41.7%	42.9%
92	(2)	> 3	8	35217	762	41.6%	42.8%
93	3	1	31	35279	765	41.5%	42.7%
94	3	1	30	35339	768	41.4%	42.6%
95	11	2	6	35399	779	41.3%	42.6%
96	6	2	12	35459	785	41.2%	42.5%
97	21	7	3	35519	806	41.1%	42.4%
98	5	1	14	35575	811	41.0%	42.3%
99	5	1	14	35631	816	40.9%	42.2%
100	5	1	14	35687	821	40.8%	42.2%

101	5	1	14	35743	826	40.7%	42.1%
102	5	1	14	35799	831	<b>4</b> 0.6%	42.0%
103	5	1	14	35855	836	40.5%	41.9%
104	5	1	14	35911	841	40.4%	<b>4</b> 1.8%
105	5	1	14	35967	846	40.30	41.7%
106	9	3	7	36023	855	A0.240	√ 41.7%
107	12	3	5	36078	867	40.190	41.6%
108	12	3	5	36133	879	40.1%	41.5%
109	12	3	5	36188	861	10.0%	41.4%
110	12	3	5	36243	793	> <sup>39.9%</sup>	41.4%
111	12	3	5	36298	915 /	× 39.8%	41.3%
112	12	5	5	36353		39.7%	41.2%
113	3	1	27	36467	930	39.6%	41.1%
114	3	1	27	36461	933	39.5%	41.1%
115	3	1	26	√365 <b>13</b>	936	39.4%	41.0%
116	5	1	13	( <del>1</del> 3555 )	941	39.3%	40.9%
117	5	1	13	30617	946	39.2%	40.8%
118	6	2	1d(	36667	952	39.2%	40.7%
119	8	4	<i>/</i> 27	<u>3</u> 6716	960	39.1%	40.7%
120	5	1	12	> 36764	965	39.0%	40.6%
121	7	1 🏠	8	36812	972	38.9%	40.5%
122	13	5/-	4	36860	985	38.8%	40.5%
123	3	1	23	36906	988	38.8%	40.4%
124	6	[//2	>> 9	36951	994	38.7%	40.3%
125	16	The same of the sa	3	36996	1010	38.6%	40.3%
126	5 ((	18/2	11	37040	1015	38.5%	40.2%
127	12	<i>J</i>	4	37084	1027	38.5%	40.2%
128	12	4	4	37128	1039	38.4%	40.1%
		>					